New Technique of Near Maximum Likelihood Detection Processes

AL-Rawi Muhanned¹, AL-Rawi Muaayed²

¹University of Ibb, Yemen ²AL-Mustansiryia University, Iraq

E-mail: muhrawi@yahoo.com

This paper introduces new detector named newly adaptively designed near maximum likelihood detector (NADD). This detector combines adaptively three types of near maximum likelihood detectors, pseudobinary, pseudoquaternary, and pseudooctonary. The performances of NADD, pseudobinary, pseudoquaternary, and pseudooctonary detectors are measured using data transmission at 9.6 kb/s over telephone channel. Simulation results show that the performance of NADD is better than the performances of pseudobinary, and pseudoquaternary detectors, but little bit worse than the performance of pseudooctonary detector.

Key words: Intersymbol interference; Near maximum likelihood detector; Adaptive detection

Introduction

The Maximum Likelihood Sequence Detector(MLSD) is a procedure for estimating a sequence of bits from a sequence of channel output observables, given a model of the communication system. In the presence of Intersymbol Interference(ISI), the Viterbi algorithm(VA) provides an efficient way of computing the MLSD [1, 2]. However, the VA still becomes impractical when the time spread of the ISI is large because of the exponential relation between ISI time spread and VA complexity.

One way of reducing the complexity of Viterbi detector is by giving the VA an approximate channel model with a shorter time spread than that of the original channel. Considerable researches have used this way to achieve the performance of the VA at reduced complexity [3–18].

Another way which is considered in this paper is to use detectors called Near Maximum Likelihood Detectors [19–26]. These detectors operate similarly to Viterbi algorithm, but using different selection process for the stored sequences of possible data symbol values, and only a very few of these sequences are stored with the corresponding costs.

1 Data transmission system

Fig. 1 shows the model of data transmission system. The first part in this model is random data generator which generates binary data, and each 4-bit is mapped into one of 16-point QAM constellation. Thus, the output of random data generator is data symbols $\{s_i\}$, and the possible values of s_i are given by all combination of ± 1 ,

 ± 3 , & $\pm j_1$, $\pm j_3$ where $j = \sqrt{-1}$. Then, the data symbols $\{s_i\}$ enter the Quadrature Amplitude Modulation(QAM) transmitter which consists of transmitter filter and QAM modulator. The transmitter filter is a low-pass filter performs the function of limiting the signal spectrum before modulation process.



Fig. 1. Model of data transmission system

The resulting output of the QAM transmitter is QAM signal with carrier frequency of 1800 Hz and symbol rate of 2400 baud giving an information rate of 2400×4 bits = 9600 b/s. The output of the QAM transmitter passes through telephone channel, and Additive White Gaussian Noise (AWGN) added to the signal before entering the QAM receiver. The QAM receiver consists of QAM demodulator and receiver filter. The receiver filter is a low-pass filter used in combination with the transmitter filter to produce realistic levels of intersymbol interference. The output of QAM receiver is data symbols $\{r_i\}$ used by the Least Mean Square (LMS) estimator to estimate the sampled impulse response (SIR) of baseband telephone channel. Finally, the data symbols $\{r_i\}$ and SIR are used by the detector to obtain the detected symbols $\{s'_i\}$.

2 Detector model

2.1 Pseudo-binary, -quaternary, -octonary detector

The pseudobinary detector (BD), pseudoquaternary detector (QD) [20], and pseudooctonary detector (OD) [24] are described as follows.

Just prior to the receipt of the signal sample r_i at time t = iT, the detector holds in store k (*n*-component) vectors Q_{i-1} given below (k = 2 for pseudobinary, k = 4for pseudoquaternary and k = 8 for pseudoctonary),

$$Q_{i-1} = \begin{bmatrix} x_{i-n} & x_{i-n+1} & \dots & x_{i-1} \end{bmatrix}$$
(1)

where x_i is possible value of s_i .

Each stored vector is associated with a cost U_{i-1} given by

$$U_{i-1} = \sum_{j=0}^{i-1} \left| r_j - \sum_{h=0}^g x_{(j-h)} \nu_h \right|^2 =$$
$$= \sum_{j=0}^{i-2} \left| r_j - \sum_{h=0}^g x_{(j-h)} \nu_h \right|^2 + w_{i-1} =$$
$$= U_{i-2} + w_{i-1} \quad (2)$$

where $\{v_h\}$ is the sampled impulse response of baseband telephone channel (estimated by LMS estimator) having length of (g + 1) (where g < n), and w_{i-1} is the corresponding estimate of the noise component in the received sample r_{i-1} .

On the receipt of the signal sample r_i , the detector expands every vector Q_{i-1} into four (n+1) components vectors $\{P_i\}$, given below, having smallest cost. The selection of P_i is achieved through the use of simple threshold-level comparison and does not involve the computation of any costs.

$$P_i = \begin{bmatrix} x_{i-n} & x_{i-n+1} & \dots & x_i \end{bmatrix}$$
(3)

The first *n*-components of P_i are as shown in the original vector Q_{i-1} and the last component x_i takes

85

on any one of the four different values of its 16 possible values. In pseudobinary, the number of expanded vectors is 8 (see Fig. 2), in pseudoquaternary is 16 (see Fig. 3), while, in pseudooctonary is 32 (see Fig. 4). Then the detector evaluates for each expanded vector P_i its cost given by

$$U_{i} = U_{i-1} + \left| r_{i} - \sum_{h=0}^{g} x_{(i-h)} \nu_{h} \right|^{2} = U_{i-2} + w_{i-1} + w_{i} \quad (4)$$

The detector then selects the vector P_i with the smallest cost and takes its first component x_{i-n} as the detected value s'_{i-n} of the data symbol s_{i-n} .

All vectors $\{P_i\}$ for which $s'_{i-n} \neq x_{i-n}$ are discarded, and the first components of all remaining vectors are omitted to give the corresponding *n*-component vectors $\{Q_i\}$ where

$$Q_i = [x_{i-n+1} \ x_{i-n+2} \ \dots \ x_i]$$
 (5)

The detector then selects from the resulting vectors $\{Q_i\}$ the k vectors with the lowest costs $\{U_i\}$. The k vectors $\{Q_i\}$ together with their costs are stored in preparation for the next detection cycle.



Fig. 2. Configuration of pseudobinary detector

After each detection process, and to prevent overflow due to the increase in costs over any transmission, the smallest cost is subtracted from the cost of each vector, so that the value of the smallest cost is always reduced to zero.

The starting up procedure for the detector begins with k stored vectors $\{Q_{i-1}\}$ that are all the same and correct. A zero cost is allocated to one of the k vectors and a very high cost to each of the remaining vectors. After a few received samples, the detector holds k vectors which are all different and are all derived from the original vector with zero cost.



Fig. 3. Configuration of pseudoquaternary detector



Fig. 4. Configuration of pseudooctonary detector

2.2 Newly adaptively designed detector

This newly adaptively designed detector (NADD) combines adaptively BD, QD, and OD. The value of k

changes between 2, 4, and 8 which is assigned every time a signal sample r is received (see Fig. 5). One criteria of assigning the value of k is given below,

$$k = \begin{cases} 2 & if(w_i)_{min} \leq \frac{1}{2} \begin{bmatrix} \frac{(w_{i-3})_{min} + (w_{i-2})_{min} + (w_{i-1})_{min}}{3} \\ 4 & if(w_i)_{min} > \frac{1}{2} \begin{bmatrix} \frac{(w_{i-3})_{min} + (w_{i-2})_{min} + (w_{i-1})_{min}}{3} \end{bmatrix} \\ and \leq \begin{bmatrix} \frac{(w_{i-3})_{min} + (w_{i-2})_{min} + (w_{i-1})_{min}}{3} \end{bmatrix} \\ 8 & if(w_i)_{min} > \begin{bmatrix} \frac{(w_{i-3})_{min} + (w_{i-2})_{min} + (w_{i-1})_{min}}{3} \end{bmatrix} \end{cases}$$

$$(6)$$

The above criterion assigns the value of k depending on comparison between the current minimum value of w and the average or half of the average of previous three minimum values of w. When the value of $(w_i)_{min}$ increases, more vectors are needed to be evaluated, so kincreases too, and vice versa.



Fig. 5. Newly adaptively designed detector

The detector needs to store $(w_{i-3})_{min}$, $(w_{i-2})_{min}$, and $(w_{i-1})_{min}$ before subtracting the cost of any vector from the smallest cost.

The starting up procedure begins with k = 8 vectors that are all the same and correct. A zero cost is allocated to one of the eight vectors and a very high cost to each of the remaining seven. The initial values of $(w_{i-3})_{min}$, $(w_{i-2})_{min}$, and $(w_{i-1})_{min}$ are zero.

3 Simulation results

A series of computer simulation tests have been carried out on the system in Fig. 1 with four types of detectors, BD, QD, OD, and NADD to determine their relative tolerance to AWGN when operating over telephone channel.

The performance of the whole system is measured by drawing symbol error rate (SER) versus signal-to-noise ratio (SNR). The SER is given by

SER = NEDS/NTS

where NEDS is the number of erroneous detected samples & NTS is the number of total transmitted samples.

Fig. 6 shows comparison among the four detectors. It seems that at error rate of 10^{-5} , the performance of NADD is better than the performance of BD by approximately 0.6 dB, and better than the performance of QD by approximately 0.2 dB, but worse than the performance of OD by approximately 0.1 dB.



Fig. 6. Error rate perfomance

Conclusion

A new detector was developed to mitigate the ISI introduced by the communication channel. This detector which is named NADD combines adaptively three detectors BD, QD, and OD. So, the three detectors can be replaced by one detector which leads to reduce the complexity of whole detector model. Simulation results show that the performance of NADD is better than that for BD and QD but little bit worse than that for OD.

References

 Forney G. (1972) Maximum likelihood sequence estimation of digital sequences in the presence of ISI, *IEEE Transactions* *on Information Theory*, Vol. 18, No. 3, pp. 363-378. DOI: 10.1109/tit.1972.1054829

- [2] Forney G. (1973) The Viterbi algorithm, *Proceedings of the IEEE*, Vol. 61, No. 3, pp. 268-278. DOI: 10.1109/PROC.1973.9030
- Falconer D. and Magee F. (1973) Adaptive channel memory truncation for maximum likelihood sequence estimation, *Bell System Technical Journal*, Vol. 52, No. 9, pp. 1541-1562. DOI: 10.1002/j.1538-7305.1973.tb02032.x
- [4] Beare C. (1978) The choice of the desired impulse response in combined linear-Viterbi algorithm equalizers, *IEEE Transactions on Communications*, Vol. 26, pp. 1301-1307. DOI: 10.1109/TCOM.1978.1094214
- [5] Bergmans J.W.M., Rajput S.A. and van De Laar F.A.M. (1987) On the use of decision feedback for simplifying the Viterbi detector, *Philips Journal of Research*, Vol. 42, No. 4, pp. 399-428.
- [6] Qureshi S. and Eyubolu M. (1988) Reduced state sequence estimation with set partitioning and decision feedback, *IEEE Transactions on Communications*, Vol. 36, No. 1, pp. 13-20. DOI: 10.1109/26.2724
- [7] Duel-Hallen A. and Heegard C. (1989) Delayed decision-feedback sequence estimation, *IEEE Transactions on Communications*, Vol. 37, No. 51, pp. 428-436. DOI: 10.1109/26.24594
- [8] Sundstrom N., et al. (1994) Combined linear-Viterbi equalizer: Comparative study and a minimax design, Proc. of 44th IEEE Vehicular Technology Conference. DOI: 10.1109/VETEC.1994.345297
- [9] Kamel R. and Bar-Ness Y. (1996) Reduced complexity sequence estimation using state partitioning, *IEEE Transactions on Communications*, Vol. 44, No. 9, pp. 1057-1063. DOI: 10.1109/26.536909
- [10] Takizawa K. and Kohno R. (2005) Low complexity Viterbi equalizer for MBOK DS-UWB systems, *IEICE Transacti*ons on Fundamentals of Electronics, Communications and Computer Sciences, Vol. E88-A, No. 9., pp.2350-2355. DOI: 10.1093/ietfec/e88-a.9.2350
- [11] Chien-cheng T. (2007) Symbol-based decision feedback equalizer with maximum likelihood sequence estimation for wireless receivers under multipath channels, Patent US7197094.
- [12] Myburgh H. and Olivier J. (2009) Low complexity iterative MLSE equalization of M-QAM signals in extremely long Rayleigh fading channels, *Proc. IEEE EUROCON*, Saint-Petersburg, Russia. DOI: 10.1109/eurcon.2009.5167861
- [13] Peng Y. et al. (2010) Complexity and performance tradeoffs of near-optimal detectors for cooperative ISI channels, *Proc.* of *IEEE International Conference on Military Communicati*ons. DOI: 10.1109/milcom.2010.5680238
- [14] Stephen A. and Quinn L. (2010) High performance equalizer having reduced complexity, Patent US 20100202507.
- [15] Turner-Barnes A. and Bibyk S. (2010) Is hybrid combination of Viterbi detector and decision feedback equalizer feasible in electrical SerDes?, *Design Con-2010*, Ohio State University, USA.
- [16] Rusek F. and Prlja A. (2012) Optimal channel shortening for MIMO and ISI channels *IEEE Transaction. Wireless Communications*, Vol. 11, No. 2, pp. 810-818. DOI: 10.1109/twc.2011.121911.110809

- [17] Maggio G.N., Hueda M.R. and Agazzi O.E. (2014) Reduced complexity MLSD receivers for nonlinear optical channels, *IEEE Photonics Technology Letters*, Vol. 26, No. 4, pp.398-401. DOI: 10.1109/lpt.2013.2295200
- [18] Zheng N. and Zhang T. (2015) Design of Low-Complexity 2-D SOVA Detector for Shingled Magnetic Recording, *IEEE Transactions on Magnetics*, Vol. 51, No. 4, pp. 1-7. DOI: 10.1109/tmag.2014.2362882
- [19] Clark A.P. and Clayden M. (1984) Pseudobinary Viterbi detector. *IEE Proceedings F Communications, Radar and Signal Processing*, Vol. 131, No. 2, pp. 208-218. DOI: 10.1049/ip-f-1.1984.0034
- [20] Clark A.P. (1985) Pseudobinary and pseudoquaternary detection processes for linearly distorted multilevel QAM signals. *IEEE Transactions on Communications*, Vol. 33, No. 7, pp. 639-645. DOI: 10.1109/tcom.1985.1096351
- [21] Clark A.P. and Abdullah S.N. (1987) Near maximum likelihood detectors for voiceband channels. *IEE Proceedings*, Vol. 134, No. 3, pp. 217-226. DOI: 10.1049/ip-f-1.1987.0047
- [22] Abdullah S. N. (2009) Improved data detection processes using retraining over telephone lines. *Journal of Engineering*, Vol. 15, No. 1, pp. 3336-3346.
- [23] AL-Rawi M. and AL-Rawi M. (2012) Equalized near maximum likelihood detector. *Radioelectronics* and *Communications Systems*, Vol. 55, No. 12, pp. 568-571. doi: 10.3103/S0735272712120072. DOI: 10.3103/s0735272712120072
- [24] AL-Rawi, M., and M. AL-Rawi. 2013. "Pseudooctonary near maximum likelihood detector. *Radioelectronics and Communications Systems*, Vol. 56, No. 9, pp. 460-463. DOI: 10.3103/S0735272713090069.
- [25] AL-Rawi M. and AL-Rawi M. (2015) Pseudohexadecimal near maximum likelihood detector. *Pacific Science Review* A: Natural Science and Engineering, Vol. 17, Issue 3. DOI: 10.1016/j.psra.2015.12.003
- [26] AL-Rawi M. and AL-Rawi M. (2016) Adaptive near maximum likelihood detector. *International Review of Appli*ed Sciences and Engineering, Vol. 7, Issue 1. DOI: 10.1556/1848.2016.7.1.1

Новий підхід до реалізації декодера квазімаксимальної правдоподібності

Муханнед Аль-Раві, Муаайед Аль-Раві

В роботі представлений новий адаптивний детектор квазімаксимального правдоподібності (НАДКП). Цей детектор представляє собою адаптивне поєднання в собі трьох типів детекторів максимальної правдоподібності: псевдобінарного, псевдочетвертного і псевдовісімкового. Продуктивність НАДКП, псевдобінарного, псевдочетверічного і псевдовосьмерічного детекторів виміряна за допомогою передачі даних по телефонному каналу на швидкості 9.6 кб/с. Результати моделювання показали, що продуктивність НАДКП краща, ніж у псевдобінарного і псевдочетвертного детекторів, але трохи гірша ніж продуктивність псевдовісімкового детектора.

Ключові слова: міжсимвольна інтерференція; детектор квазімаксимальної правдоподібності; адаптивне виявлення

Новый подход к реализации декодера квазимаксимального правдоподобия

Муханнед Аль-Рави, Муаайед Аль-Рави

В работе представлен новый адаптивный детектор квазимаксимального правдоподобия (НАДКП). Этот детектор представляет собой адаптивное сочетание в себе трех типов детекторов максимального правдоподобия: псевдобинарного, псевдочетверичного и псевдовосьмеричного Производительность НАДКП, псевдобинарного, псевдочетверичного и псевдовосьмеричного детекторов измеряна с помощью передачи данных по телефонному каналу на скорости 9.6 кб/с. Результаты моделирования показали, что производительность НАДКП лучше, чем у псевдобинарного и псевдочетверичного детекторов, но немного хуже чем производительность псевдовосьмеричного детектора.

Ключевые слова: межсимвольная интерференция; детектор квазимаксимального правдоподобия; адаптивное обнаружение